

Part 1: Factoring

When factoring we want to find numbers that multiply to c!

that also add to b! $[ax^2 + bx + c]$

Example: $x^2 - 2x - 8$

$(x-4)(x+2)$

$$\begin{array}{r} -8 \\ \hline -4 \cdot 2 \\ -8 \cdot 1x \end{array} \quad \begin{array}{r} -8 \\ \hline -2 \cdot 4x \\ 8 \cdot -1x \end{array}$$

Factor the following quadratics:

1. $x^2 + 8x + 12$

$(x+6)(x+2)$

$$\frac{12}{6 \cdot 2}$$

2. $x^2 - x - 12$

$(x-4)(x+3)$

$$\frac{-12}{6 \cdot 2} \\ 3 \cdot -4$$

3. $x^2 + 6x - 16$

$(x+8)(x-2)$

$$\frac{16}{8 \cdot -2}$$

4. $x^2 + 8x + 15$

$(x+5)(x+3)$

$$\frac{15}{5 \cdot 3}$$

5. $x^2 - 11x + 24$

$(x-8)(x-3)$

$$\frac{24}{-8 \cdot -3}$$

6. $x^2 + 5x - 14$

$(x+7)(x-2)$

$$\frac{14}{-2 \cdot 7}$$

7. $x^2 + 4x - 32$

$(x+8)(x-4)$

$$\frac{32}{8 \cdot -4}$$

8. $x^2 - 25$

$(x+5)(x-5)$

$$\frac{25}{-5 \cdot -5}$$

To Find factors on your calculator $y = \# / x$

Difference of Squares!

Part 2: Complete the Square

When completing the square we want to divide "b" by 2!

Next we want to square that & subtract from back.

Example: $y = x^2 - 12x + 28 - 36$

$$\downarrow$$

$$\frac{-12}{2} = (-6)^2 = 36$$

$$(x - 6)^2 - 8$$

Complete the square for the following quadratics:

1. $y = x^2 + 12x + 20 - 36$

$$\downarrow$$

$$\frac{12}{2} = (6)^2 = 36$$

$$(x + 6)^2 - 16$$

2. $y = x^2 - 10x - 15 - 25$

$$\downarrow$$

$$\frac{-10}{2} = (-5)^2 = 25$$

$$(x - 5)^2 - 40$$

5. $y = x^2 + 4x + 3 - 4$

$$\downarrow$$

$$\frac{4}{2} = (2)^2 = 4$$

$$(x + 2)^2 - 1$$

2. $y = x^2 + 8x + 16 - 16$

$$\downarrow$$

$$\frac{8}{2} = (4)^2 = 16$$

$$(x + 4)^2 + 0$$

Not needed!

4. $y = x^2 - 18x + 80 - 81$

$$\downarrow$$

$$\frac{-18}{2} = (-9)^2 = 81$$

$$(x - 9)^2 - 1$$

6. $y = x^2 - 16x + 200 - 64$

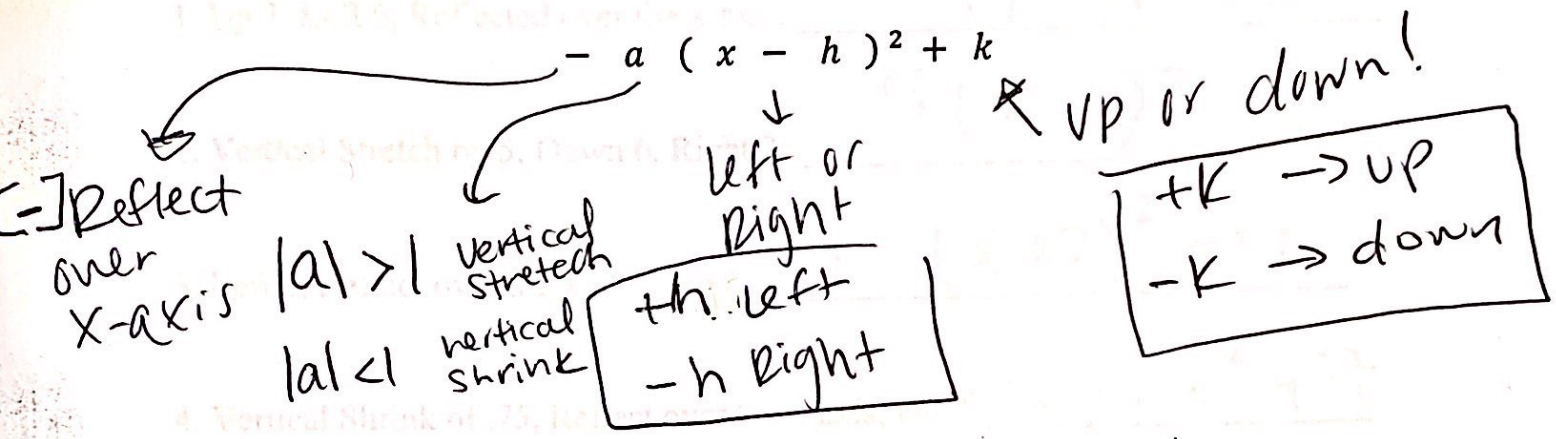
$$\downarrow$$

$$\frac{-16}{2} = (-8)^2 = 64$$

$$(x - 8)^2 + 136$$

Part 3: Vertex Form

We can describe transformations given the vertex form equation by using the following rules.



Vertex: (h, k) LOS: $x = h$

don't forget to change sign of h!

State the transformations given the following quadratics:

1. $y = -2(x-1)^2 + 1$

- Reflect over x-axis
- vertical stretch by 2
- Right 1
- Up 1

2. $y = .25(x+3)^2 - 5$

- vertical shrink by $\frac{1}{4}$ [.25]
- Left 3
- Down 5

3. $y = -(x+6)^2 + 4$

- Reflect over x-axis
- Left 6
- Up 4

4. $y = 3(x-1)^2 - 2$

- vertical stretch by 3
- Right 1
- Down 2

5. $y = .5x^2 - 7$

- vertical shrink by $\frac{1}{2}$ [.5]
- Down 7.

6. $y = -(x+4)^2$

- Reflect over x-axis
- Left 4

Write the equation of the quadratic where the parent function has been translated:

1. Up 3, Left 6, Reflected over the x-axis: $-(x+6)^2 + 3$

2. Vertical Stretch by 5, Down 6, Right 2: $5(x-2)^2 - 6$

3. Left 2, Reflect over the x-axis, Up 4: $-(x+2)^2 + 4$

4. Vertical Shrink of .75, Reflect over the x-axis, Up 7: $-.75x^2 + 7$

State the vertex and line of symmetry of the following:

1. $y = -2(x - 1)^2 + 1$

Vertex: $(1, 1)$ LOS: $x = 1$

2. $y = .25(x + 3)^2 - 5$

Vertex: $(-3, -5)$ LOS: $x = -3$

3. $y = -(x + 6)^2 + 4$

Vertex: $(-6, 4)$ LOS: $x = -6$

4. $y = 3(x - 1)^2 - 2$

Vertex: $(1, -2)$ LOS: $x = 1$

5. $y = .5x^2 - 7$

Vertex: $(0, -7)$ LOS: $x = 0$

6. $y = -(x + 4)^2$

Vertex: $(-4, 0)$ LOS: $x = -4$

Part 4: Graphing Quadratics

We can determine a quadratic function easily by looking at a graph!

Quadratic Functions in Vertex Form and Factored Form:

First we want to identify the location of the vertex (min/max point)

Or x-intercepts (where it crosses x-axis):

When putting it in the equation don't forget to change the sign of x.

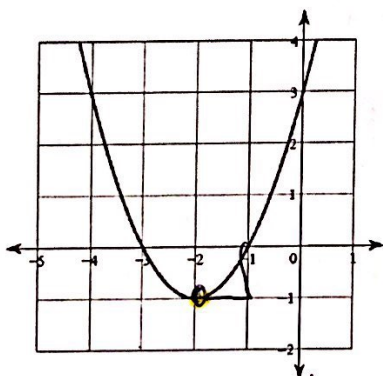
Next we want to determine if there have been any stretches/shrinks!

We can do this by going to vertex, 1 to the right → Go up/down that value is a!

Lastly, check for Reflection by looking to see if your graph is flipping.

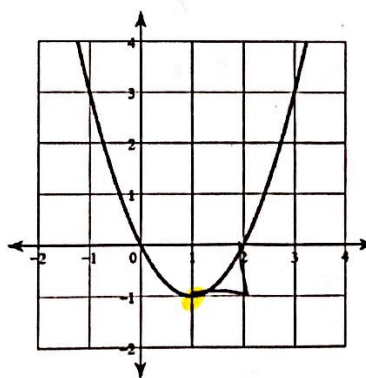
State the quadratic function for the following in Vertex Form:

1.



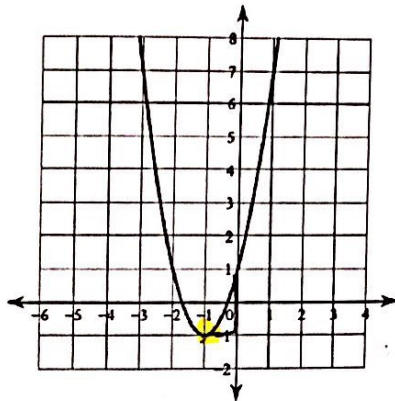
$(x + 2)^2 - 1$

2.



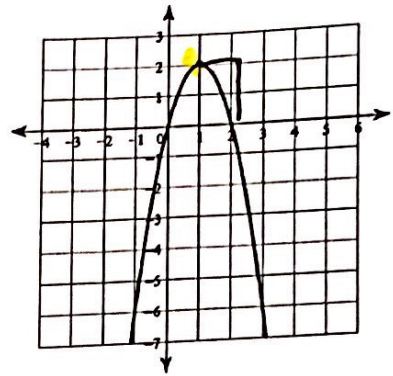
$(x - 1)^2 - 1$

3.



$$2(x+1)^2 - 1$$

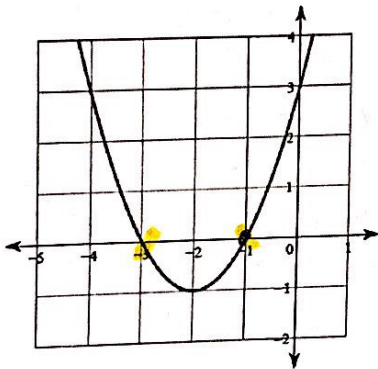
4.



$$-2(x-1)^2 + 2$$

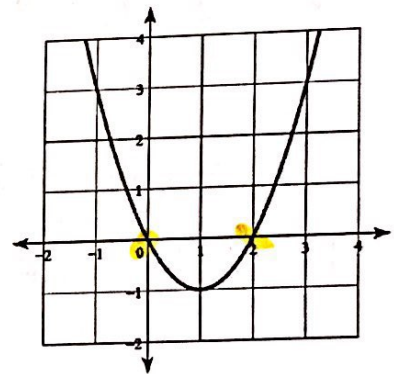
State the quadratic function for the following in Factored Form:

5.



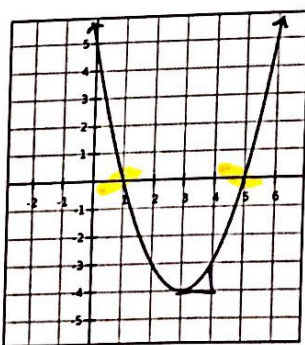
$$(x+1)(x+3)$$

6.



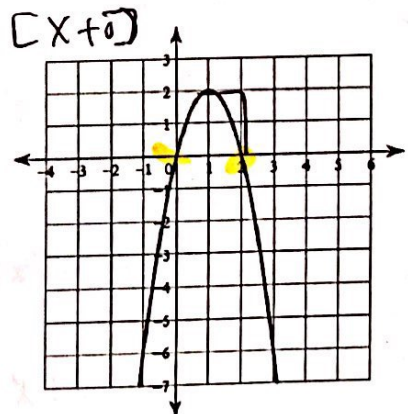
$$(x)(x-2)$$

7.



$$(x-1)(x-5)$$

8.



$$-2(x)(x-2)$$