Unit 5 – Solving Quadratic Functions

Now that we know how to work with quadratics, we can solve them! What does it mean when we solve a quadratic? What are we looking for?

Since we have quadratics we should be looking for ______solutions!

We can write our solutions as ordered pairs. (#, 0) (#,0) or as _____

Solving Methods:

-Factoring/Zero Product Property

-Square Root Method

-Quadratic Formula

Today we will talk through helping us find the best strategy depending on the quadratics we are given.

<u>**Part 1- Factoring (Zero Product Property) Method:**</u> If quadratics are factored, or if we can feel confident in our ability to factor a given problem, this method can be super easy!

| All we need to do is | | and solve for x! |
|-----------------------|----------------------|------------------|
| 1. $(x-2)(x+4)$ | 2. $(2x - 3)(x - 5)$ | 3. x (3x +2) |
| | | |
| | | |
| 4. $(x + 12) (x - 6)$ | 5. (x – 7) (2x – 5) | 6. x(x+9) |
| | | |
| | | |
| 7. $(x+5)(x-15)$ | 8. $(x-3)(x-8)$ | 9. (x+6)(x+3) |

In order to solve using the remaining methods we need to recall:

| Simplifying Radicals: When simplifying radicals it is important that we make | | | | | |
|---|------------------------------|--------|---------------|---------------------|---|
| We want to look for | | | | | |
| Anything left | | | | | · |
| If multiple numbers are p | present in either location v | ve mus | st | | · |
| Remember, negatives under the radical mean that we have | | | | | · |
| Simplify the following radicals completely. | | | | | |
| 1. \sqrt{250} | $2.\sqrt{48}$ | 3. | $\sqrt{-16}$ | 4. √ <u>216</u> | |
| | | | | | |
| | | | | | |
| 5. $\sqrt{45}$ | 6. √ − 98 | 7. | $\sqrt{-169}$ | 8. √ 200 | |
| Part 2- Square Root Method: If quadratics are in, (or | | | | | |
| that we find confident putting it in this form) or a quadratic is, this is the best method! | | | | | |

1. $(x+3)^2 + 2 = -10$ 2. $2(x+2)^2 + 24$

3.
$$5x^2 - 1 = 9$$

4. $(x - 4)^2 - 13 = 0$

5. $5 - 3x^2 = 20$ 6. $x^2 - 49$

7. $x^2 + 100$ 8. $2(x+3)^2 + 12 = 4$

$$9.5x^2 + 9 = 134 10.2x^2 + 8 = 10$$

<u>Part 3- The Quadratic Formula:</u> If quadratics have an a-value that is bigger than one, or we do not know how to approach in solving, the quadratic formula can always work!

State the Quadratic Formula:

To help you remember, you could sing our song... or think about this story! "There once was a <u>negative</u> **b**oy who was <u>unsure</u> if he wanted to go to <u>a radical party</u>. But the **b**oy was feeling <u>squared</u> and <u>missed out</u> on <u>four</u> **a**wesome **c**hicks! The party was not <u>over until</u> **2 a**m!

x = ——

| Solving using the Quadratic Formula: | |
|--------------------------------------|------------------------|
| $1. x^2 + 16x + 68 = 0$ | 2. $2x^2 - 7x + 6 = 0$ |

a= ____ b=____ c=____

a=_____b=_____c=____

3.
$$x^2 - 8x + 24 = 0$$
 4. $2x^2 - 32 = 0$

a= ____ b=___ c=___

a= ____ b=____ c=____

5. $6x^2 + 2x + 1 = 0$

6. $x^2 + 5x - 6 = 0$

a=_____b=_____c=____

Calculator Strategies:

- We can also try to use our calculator while testing to help us find solutions!
 - Use your table! We want to look for _____
 - Careful: Not all answers can be seen from the table.

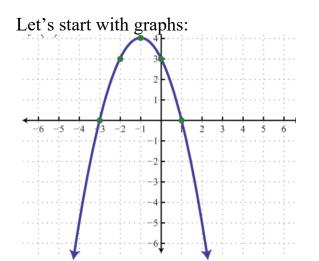
| Example: $x^2 - x - 6$ | | |
|------------------------|------|--|
| Solutions: | | |

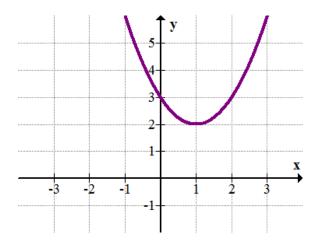
- Trace Feature: We can trace in our calculators to find where the x-intercepts are. We can then use those values to match- up our answer choices.
 - Steps:
 - $2^{nd} \rightarrow Trace$
 - Zero
 - Left Bound, Right Bound, Enter!

Example: $3x^2 - 5x - 15$

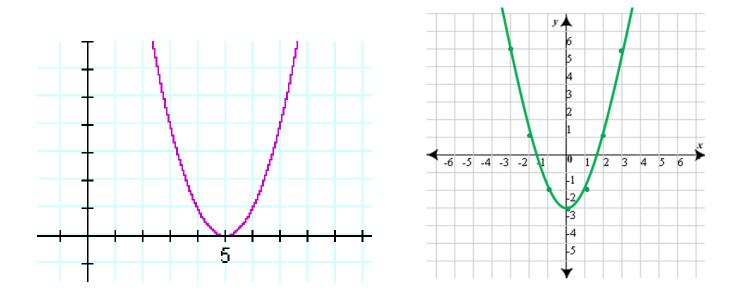
Solutions: _____

Types of solutions: We can look at our graph as well as the ______ of a quadratic to tell us the types of solutions! Let's take a look to see how this works!





!



Let's look at Discriminants! (Fancy way of using what we have in the quadratic formula!)

We will use: _____

| | Discriminant | Type of Solution |
|--------------------------|--------------|------------------|
| 1. $y = 3x^2 - 3x + 2$ | | |
| | | |
| | | |
| 2. y= $x^2 - 10x + 1$ | | |
| | | |
| | | |
| 3. $y=2x^2-16x+24$ | | |
| | | |
| $4 - x - a^2 + 4a + 17$ | | |
| 4. $y = x^2 + 4x + 17$ | | |
| | | |
| 5. $y = x^2 + 2x - 6$ | | |
| $3 \cdot y = x + 2x = 0$ | | |
| | | |
| | | |
| 6. $y = 2x^2 - x - 3$ | | |
| | | |
| | | |
| | | |